



**M:** Course Objectives / Learning Outcomes

General comments: MATH 1220 is a second course in calculus. The four-semester sequence of MATH 1120, 1220, 2321, and 2421 provides the foundation for continued studies in science, engineering, computer science, or a major in mathematics.

Specific objectives:

At the conclusion of this course, the student should be able to:

- compute finite Riemann sums and use to estimate area
- form limits of Riemann sums and write the corresponding definite integral
- recognize and apply the Fundamental Theorem of Calculus
- evaluate integrals involving exponential functions to any base
- evaluate integrals of reciprocal functions
- evaluate integrals involving basic trigonometric functions and integrals whose solutions require inverse trigonometric functions
- be able to choose an appropriate method and apply the following techniques to finding antiderivatives and evaluate definite integrals:
  - a) integration by parts
  - b) trigonometric and rationalizing substitution
  - c) completing the square for integrals involving quadratic expressions
  - d) partial fractions
  - e) integrals of products of trigonometric functions
- apply integration to problems involving areas, volumes, arc length, work, velocity and acceleration
- be able to determine the convergence or divergence of improper integrals by comparison test
- determine if a given sequence converges or diverges
- determine if a sequence is bounded and/or monotonic
- determine the sum of a geometric series
- be able to choose an appropriate test and determine series convergence/divergence using:
  - a) integral test
  - b) simple comparison test
  - c) limit comparison test
  - d) ratio and root test
  - e) alternating series test
- distinguish and apply concepts of absolute and conditional convergence of a series
- determine the radius and interval of convergence of a power series
- approximate a differentiable function by a Taylor polynomial, determine the remainder term, and compute the error in using the approximation
- find a Taylor or Maclaurin series representing specified functions by:
  - a) "direct" computation
  - b) means of substitution, differentiation or integration of related power series
- find the area of a region bounded by the graph of a polar equation or parametric equations
- find the lengths of curves in polar coordinates or in parametric form
- solve first order differential equations by the method of separation of variables; apply to growth and decay problems

**N:** Course Content:

1. Introduction to the Integral
  - sigma notation
  - Riemann sums
  - the definite integral
  - the Fundamental Theorem of Calculus
  - antiderivatives; elementary substitutions
  - applications to area under and between curves, volume and work
2. Techniques of Integration
  - parts
  - trigonometric substitution

- trigonometric integrals (products and powers)
  - partial fractions (linear factors and distinct quadratic factors)
  - rationalizing substitutions
  - improper integrals
3. Applications of Integration
- areas between curves
  - volumes by slicing and cylindrical shells
  - work
  - separable differential equations
  - arc length
4. Infinite Series
- sequences
  - sum of a geometric series
  - absolute and conditional convergence
  - comparison tests
  - alternating series
  - ratio and root test
  - integral test
  - power series
  - differentiation and integration of power series
  - Taylor and Maclaurin series
  - polynomial approximations; Taylor polynomials
5. Parametric Equations and Polar Coordinates
- areas and arc lengths of curves in polar coordinates
  - areas and arc lengths of functions in parametric form
6. Optional Topics (included at the discretion of the instructor)
- tables of integrals
  - approximation of integrals by numerical techniques
  - Newton's law of cooling, Newton's law when force is proportional to velocity, and logistics curves
  - a heuristic "proof" of the Fundamental Theorem of Calculus
  - the notion of the logarithm defined as an integral
  - further applications of Riemann sums and integration
  - binomial series

**O:** Methods of Instruction

Lectures, problem sessions and assignments

**P:** Textbooks and Materials to be Purchased by Students

Stewart, Calculus: Early Transcendentals, 3rd Edition, Brooks/Cole.  
A graphing calculator is also required.

**Q:** Means of Assessment

Evaluation will be carried out in accordance with Douglas College policy. The instructor will present a written course outline with specific evaluation criteria at the beginning of the semester. Evaluation will be based on the following criteria:

1.	Weekly quizzes	0 – 40%
2.	Tests	20 – 70%
3.	Assignments	0 – 15%
4.	Attendance	0 – 5%
5.	Class participation	0 – 5%
7.	Final examination	30%

**R:** Prior Learning Assessment and Recognition: specify whether course is open for PLAR

Not open for PLAR.

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Education Council / Curriculum Committee Representative

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Dean / Director Des Wilson

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Registrar Trish Angus